

## How to use Excel® spreadsheet to carry out Monte Carlo simulation?

Monte Carlo simulation (MCS) is a method for iteratively evaluating a deterministic probability model using a very large population of random numbers as inputs. It has been proposed to be a supplement of the “Bottom-up” GUM method for evaluation of measurement uncertainty.

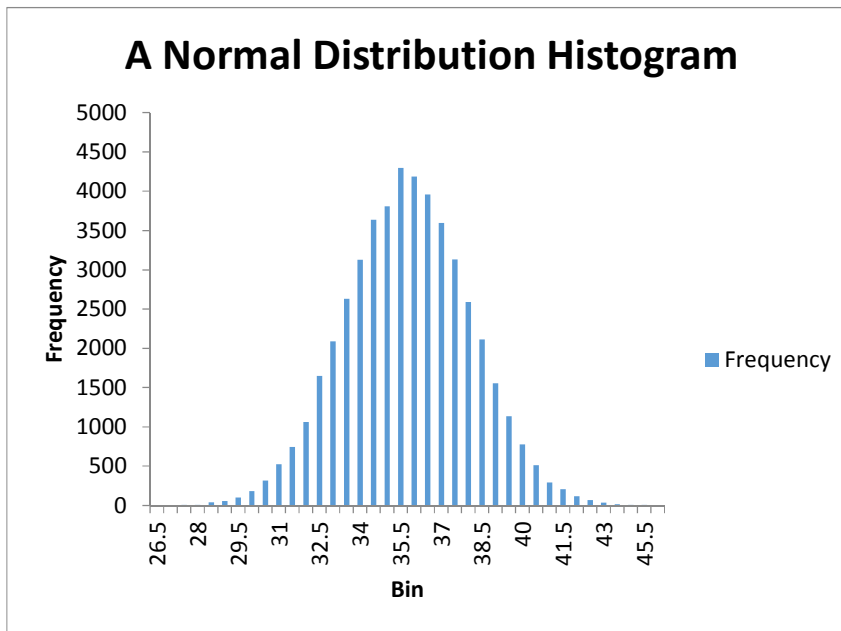
We can use a statistical software to generate such vast number of random numbers, such as Matlab®, based on a given probability distribution function. An Excel spreadsheet can also be used to carry out such calculation although it has a limited number of inputs, with a maximum of 48576 rows. However, for practical purposes, these inputs are good enough to display the probability distribution in question.

For example, given a mean of 35.5 and its standard deviation of 2.3 under the normal distribution function, we can generate some 48574 random data based on the Excel function “=NORMINV(RAND(),35.5,2.3)”

| Series | Data    |
|--------|---------|
| 1      | 33.1849 |
| 2      | 38.6867 |
| 3      | 34.9856 |
| 4      | 34.9793 |
| 5      | 36.0362 |
| 6      | 37.4078 |
| 7      | 34.9509 |
| ~      | ~       |
| 48571  | 38.6312 |
| 48572  | 38.1210 |
| 48573  | 29.5783 |
| 48574  | 34.1466 |

A histogram can be generated using the Excel Data Analysis tool tab as follows:

| Bin  | Frequency | Bin  | Frequency | Bin  | Frequency | Bin  | Frequency |
|------|-----------|------|-----------|------|-----------|------|-----------|
| 26.5 | 3         | 31.5 | 743       | 36.5 | 3960      | 41.5 | 207       |
| 27.0 | 4         | 32.0 | 1061      | 37.0 | 3595      | 42.0 | 118       |
| 27.5 | 7         | 32.5 | 1649      | 37.5 | 3134      | 42.5 | 67        |
| 28.0 | 7         | 33.0 | 2092      | 38.0 | 2587      | 43.0 | 33        |
| 28.5 | 37        | 33.5 | 2630      | 38.5 | 2113      | 43.5 | 15        |
| 29.0 | 57        | 34.0 | 3129      | 39.0 | 1555      | 44.0 | 7         |
| 29.5 | 100       | 34.5 | 3637      | 39.5 | 1135      | 45.5 | 6         |
| 30.0 | 184       | 35.0 | 3806      | 40.0 | 776       | More | 1         |
| 30.5 | 315       | 35.5 | 4295      | 40.5 | 512       |      |           |
| 31.0 | 524       | 36.0 | 4185      | 41.0 | 288       |      |           |



For a rectangular distribution function where the uncertainties are given by maximum bound within which all values are equally probable, we also can use the Excel spreadsheet to plot its data spread as described below.

For example, if we have a mean of 100 with an upper bound limit (UL) of 104 and a lower bound limit (LL) of 96 (i.e. uncertainty of  $\pm 4$ ), then we can use the function “=96+(104-94)\*RAND()” to generate thousands of random figures bounded by 96 and 104, as show in the following chart which has accumulated some 1800 data:

| Series | Data    |
|--------|---------|
| 1      | 96.077  |
| 2      | 103.419 |
| 3      | 100.317 |
| 4      | 96.077  |
| 5      | 102.801 |
| 6      | 99.975  |
| 7      | 98.261  |
| ~      | ~       |
| 1797   | 101.021 |
| 1798   | 99.421  |
| 1799   | 99.567  |
| 1800   | 99.121  |

